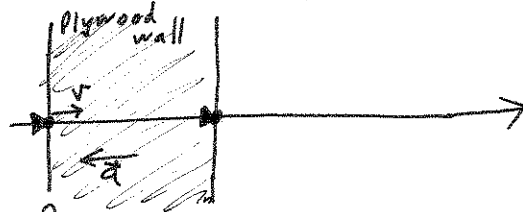


Draw & Axis the problem:



The problem has 2 parts. Let's start with part 1.

These are the conditions when the bullet first hits the wood

Bullet hits	Bullet stops
$x_0 = 0$	$x = ?$
$t_0 = 0$	$t = ?$
$v_0 = +400 \text{ m/s}$	$v = 0 \text{ m/s}$
$a_0 = -2 \times 10^6 \text{ m/s}^2$	$a = -2 \times 10^6 \text{ m/s}^2$

These are the conditions when the bullet stops.

KNOWNs: Already written explicitly above on diagram.

$$\boxed{v, v_0, a}$$

UNKNOWNs: The problem is asking for wood thickness.

Sounds like a displacement: the difference between impact ^{location} (x_0) and point where the bullet stops (x) .

$$\boxed{\Delta x} = x - x_0 = x.$$

LET'S LOOK AT MOTION EQUATIONS...

$$v^2 = v_0^2 + 2a\Delta x$$

$$v = v_0 + at$$

$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

We're looking with ~~an~~ an equation with only one unknown... particularly the unknown we need, Δx .

• The first equation above would be perfect!

$$v^2 = v_0^2 + 2a\Delta x$$

I'm going to not write units during computation because everything (all #'s here) are in meters and seconds.

$$0 = (400)^2 + 2 \cdot (-2 \times 10^6) \Delta x$$

$$0 = 1.6 \times 10^5 + (-4 \times 10^6) \Delta x$$

$$-1.6 \times 10^5 = -4 \times 10^6 \Delta x$$

$$\Delta x = \frac{-1.6 \times 10^5}{-4 \times 10^6} = \frac{1.6}{40} = \boxed{0.04 \text{ meters}}$$

Note, this is about 1.57 inches. Not much wood to stop the bullet!

Part 2... All that's changed is the initial velocity. Now, $v_0 = 800 \text{ m/s}$. Let's jump straight to solving the motion equation since the other values are the same!

$$v^2 = v_0^2 + 2a\Delta x$$

$$0 = (800)^2 + 2 \cdot (-2 \times 10^6) \Delta x$$

$$0 = 6.4 \times 10^5 - 4 \times 10^6 \Delta x$$

$$-6.4 \times 10^5 = -4 \times 10^6 \Delta x$$

$$\Delta x = \frac{-6.4 \times 10^5}{-4 \times 10^6}$$

Factors of 10 cancel to be $\frac{1}{10}$

$$\Delta x = \frac{6.4}{40}$$

$$\Delta x = 0.16 \text{ meters}$$

Note, this is about 6.3 inches. We doubled the bullet speed but have to quadruple the plywood thickness to stop this faster bullet!

